

Section
APPENDIX B

The following examples illustrate the use of life cycle analysis techniques for highway projects based on UDOT data.

Example 1

The Utah Department of Transportation is attempting to analyze the most cost effective alternative for construction of a four lane Interstate Highway. The two alternatives to be evaluated are the construction of a Portland Cement Concrete Pavement compared with the construction of an Asphaltic Concrete Pavement. The following costs per mile of construction are known for each alternative:

Portland Cement Concrete Pavement (Alternative 1)

Initial Construction Cost	\$1,200,000
Joint Sealing (year 10 & 20)	\$84,000
Routine Annual Maintenance	\$1,800
Salvage	(\$140,000)

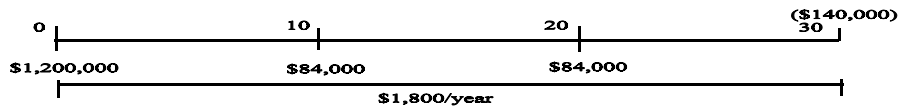
Asphaltic Concrete Pavement (Alternative 2)

Initial Construction Cost	\$900,000
Stage II Construction (year 10)	\$350,000
Recycle Pavement (year 20)	\$290,000
Routine Annual Maintenance	\$1,000
Salvage	(\$280,000)

The estimated life of each alternative is 30 years. Use a 4% discount rate to find the best alternative.

Solution:

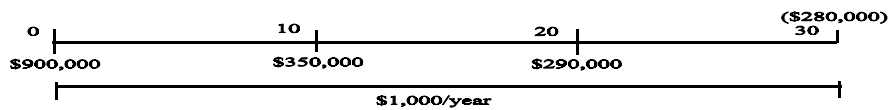
The alternative may be evaluated using either the Present Worth Method or the Annual Worth Method. Both solutions are shown. The first step is to construct a time line using the above costs. Then plug the appropriate values into the associated formula.

Alternative 1**Present Worth Method**

$$\begin{aligned}
 P &= \$1,200,000 + \$84,000 (P/F, 4\%, 10) + \$84,000 (P/F, 4\%, 20) \\
 &\quad + \$1,800 (P/A, 4\%, 30) - \$140,000 (P/F, 4\%, 30) \\
 &= 1,200,000 + 84,000 (0.6756) + 84,000 (0.4564) + 1,800 (17.2920) - 140,000 (0.3083) \\
 &= \underline{\$1,283,045} \quad \quad \quad \} \text{ ANSWER}
 \end{aligned}$$

Annual Worth Method

$$\begin{aligned}
 A &= \$1,200,000 (A/P, 4\%, 30) + \$84,000 (P/F, 4\%, 10) (A/P, 4\%, 30) \\
 &\quad + \$84,000 (P/F, 4\%, 20) (A/P, 4\%, 30) + \$1,800 - \$140,000 (A/F, 4\%, 30) \\
 &= 1,200,000 (0.0578) + 84,000 (0.6756) (0.0578) + 84,000 (0.4564) (0.0578) \\
 &\quad + 1,800 - 140,000 (0.0178) \\
 &= \underline{\$74,199} \quad \quad \quad \} \text{ ANSWER}
 \end{aligned}$$

Alternative 2**Present Worth Method**

$$\begin{aligned}
 P &= \$900,000 + \$350,000 (P/F, 4\%, 10) + \$290,000 (P/F, 4\%, 20) \\
 &\quad + \$1,000 (P/A, 4\%, 30) - \$280,000 (P/F, 4\%, 30) \\
 &= 900,000 + 350,000 (0.6756) + 290,000 (0.4564) + 1,000 (17.2920) - 280,000 (0.3083) \\
 &= \underline{\underline{\$1,199,762}} \quad \quad \quad \} \text{ ANSWER}
 \end{aligned}$$

Annual Worth Method

$$\begin{aligned}
 A &= \$900,000 (A/P, 4\%, 30) + \$350,000 (P/F, 4\%, 10) (A/P, 4\%, 30) \\
 &\quad + \$290,000 (P/F, 4\%, 20) (A/P, 4\%, 30) + \$1,000 - \$280,000 (A/F, 4\%, 30) \\
 &= 900,000 (0.0578) + 350,000 (0.6756) (0.0578) + 290,000 (0.4564) (0.0578) \\
 &\quad + 1,000 - 280,000 (0.0178) \\
 &= \underline{\underline{\$69,382}} \quad \quad \quad \} \text{ ANSWER}
 \end{aligned}$$

Comparison of Alternatives

	Alternative 1	Alternative 2
Present Worth	\$1,283,045	\$1,199,762
Annual Worth	\$74,199	\$69,382

Conclusion

As can be seen in the comparison above, Alternative 2 is the least expensive alternative. This example also illustrates that the use of either the annual worth or present worth method leads to the same conclusion.

Sensitivity Analysis**Cost Benefit Variable**

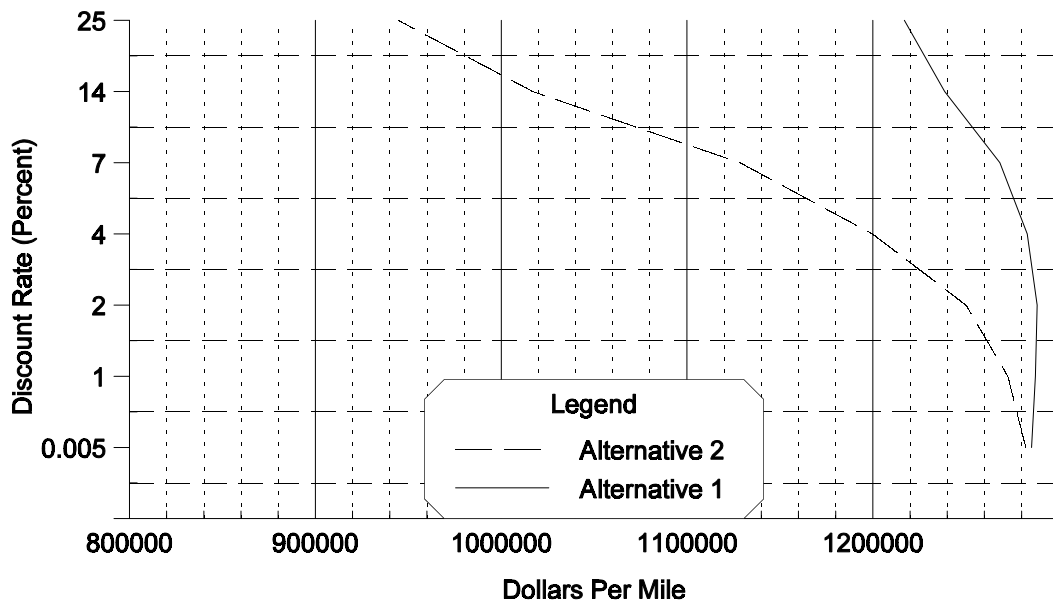
Discount Rate
 Analysis Period
 Maintenance Cost
 User Cost

<u>Present Worth Method</u> Example 1		
Discount Rate	Alternative 1	Alternative 2
0.5%	\$1,285,424	\$1,282,146
1%	\$1,287,471	\$1,272,588
2%	\$1,288,463	\$1,250,100
4%	\$1,283,045	\$1,199,762
7%	\$1,268,353	\$1,128,490
14%	\$1,238,627	\$1,017,018
25%	\$1,217,006	\$944,573

<u>Annual Worth Method</u> Example 1		
Discount Rate	Alternative 1	Alternative 2
0.5%	\$46,248	\$46,130
1%	\$49,887	\$49,310
2%	\$57,530	\$55,817
4%	\$74,199	\$69,382
7%	\$102,212	\$90,941
14%	\$176,880	\$145,233
25%	\$304,629	\$236,436

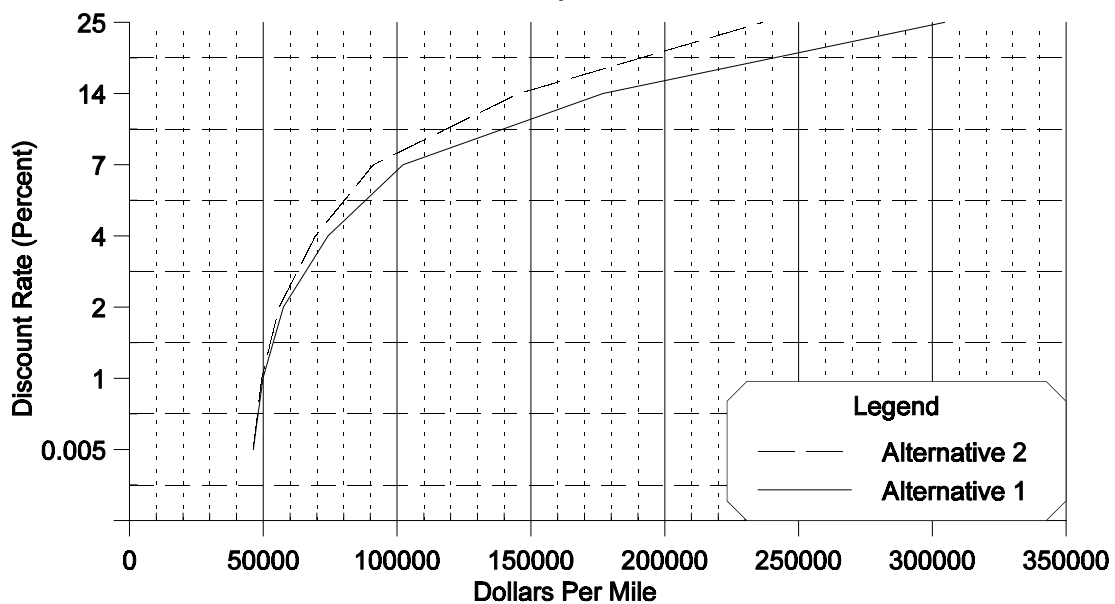
COMPARISON - PRESENT WORTH ALTERNATIVE

Example 1



COMPARISON - ANNUAL WORTH ALTERNATIVES

Example 1



Example 2

A Value Engineering Study has identified two alternative solutions for rehabilitating a principal arterial highway. Given the following information about each alternative, select the most cost effective. The following costs per mile of construction are known for each alternative:

Alternative 1

Provide a bituminous surface treatment (BST) for the next 12 years, followed by reconstruction with asphaltic concrete pavement.

BST Applications (6 year cycles)	\$97,000
Reconstruction (year 12)	\$483,000
Annual Maintenance (years 1 - 12)	16,000
Annual Maintenance (years 13-30)	4,000
Resurfacing (year 24)	\$266,000
Salvage	(\$132,000)

Alternative 2

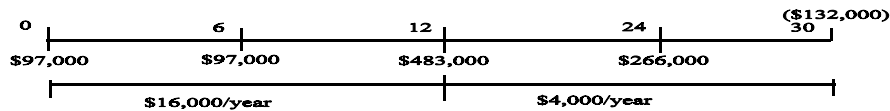
Provide reconstruction now with rehabilitation in 12 years.

Reconstruction	\$483,000
Rehabilitation (year 12)	\$306,000
Annual Maintenance (year 1 -12)	\$4,000
Annual Maintenance (year 13 - 30)	\$1,600
Resurface (year 24)	\$266,000
Salvage	\$(132,000)

The estimated life of each alternative is 30 years. Use a 4% discount rate to find the best alternative.

Solution:

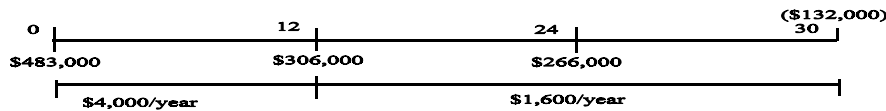
The alternative may be evaluated using either the Present Worth Method or the Annual Worth Method. Both solutions are shown. The first step is to construct a time line using the above costs. Then plug the appropriate values into the associated formula.

Alternative 1**Present Worth Method**

$$\begin{aligned}
 P &= \$97,000 + \$97,000 (P/F, 4\%, 6) + \$483,000 (P/F, 4\%, 12) + \$266,000 (P/F, 4\%, 24) + \\
 &\quad \$16,000 (P/A, 4\%, 12) + 4,000 (P/A, 4\%, 18) (P/F, 4\%, 12) \\
 &\quad - \$132,000 (P/F, 4\%, 30) \\
 &= 97,000 + 97,000 (0.7903) + 483,000 (0.6246) + 266,000 (0.3901) + 16,000 (9.3851) + \\
 &\quad 4,000 (12.6593) (0.6246) - 132,000 (0.3083) \\
 &= \underline{\$720,204} \quad \quad \quad \} \text{ ANSWER}
 \end{aligned}$$

Annual Worth Method

$$\begin{aligned}
 A &= \$97,000 (A/P, 4\%, 30) + \$97,000 (P/F, 4\%, 6) (A/P, 4\%, 30) \\
 &\quad + \$483,000 (P/F, 4\%, 12) (A/P, 4\%, 30) + \$266,000 (P/F, 4\%, 24) (A/P, 4\%, 30) \\
 &\quad + 16,000 (P/A, 4\%, 12) (A/P, 4\%, 30) + 4,000 (P/A, 4\%, 18) (P/F, 4\%, 12) \\
 &\quad (A/P, 4\%, 30) - \$132,000 (A/F, 4\%, 30) \\
 &= 97,000 (0.0578) + 97,000 (0.7903) (0.0578) + 483,000 (0.6246) (0.0578) \\
 &\quad + 266,000 (0.3901) (0.0578) + 16,000 (9.3851) (0.0578) \\
 &\quad + 4,000 (12.6593) (0.6246) (0.0578) - 132,000 (0.0178) \\
 &= \underline{\$41,650} \quad \quad \quad \} \text{ ANSWER}
 \end{aligned}$$

Alternative 2**Present Worth Method**

$$\begin{aligned}
 P &= \$483,000 + \$306,000 (P/F, 4\%, 12) + \$266,000 (P/F, 4\%, 24) \\
 &\quad + 4,000 (P/A, 4\%, 12) + \$16,000 (P/A, 4\%, 18) (P/F, 4\%, 12) \\
 &\quad - \$132,000 (P/F, 4\%, 30) \\
 &= 483,000 + 306,000 (0.6246) + 266,000 (0.3901) + 4,000 (9.3851) \\
 &\quad + 1,600 (12.6593) (0.6246) - 132,000 (0.3083) \\
 &= \underline{\underline{\$787,392}} \quad \quad \quad \} \text{ ANSWER}
 \end{aligned}$$

Annual Worth Method

$$\begin{aligned}
 A &= \$483,000 (A/P, 4\%, 30) + \$306,000 (P/F, 4\%, 12) (A/P, 4\%, 30) \\
 &\quad + \$266,000 (P/F, 4\%, 24) (A/P, 4\%, 30) + \$4,000 (P/A, 4\%, 12) (A/P, 4\%, 30) \\
 &\quad + 1,600 (P/A, 4\%, 18) (P/F, 4\%, 12) (A/P, 4\%, 30) - \$132,000 (A/F, 4\%, 30) \\
 &= 483,000 (0.0578) + 306,000 (0.6246) (0.0578) + 266,000 (0.3901) (0.0578) \\
 &\quad + 4,000 (9.3851) (0.0578) + 1,600 (12.6593) (0.6246) (0.0578) - 132,000 (0.0178) \\
 &= \underline{\underline{\$45,535}} \quad \quad \quad \} \text{ ANSWER}
 \end{aligned}$$

Comparison of Alternatives

	Alternative 1	Alternative 2
Present Worth	\$720,204	\$787,392
Annual Worth	\$41,650	\$45,535

Conclusion

As can be seen in the comparison above, Alternative 1 is the least expensive alternative. This example also illustrates that the use of either the annual worth or present worth method leads to the same conclusion.

Sensitivity Analysis**Cost Benefit Variable**

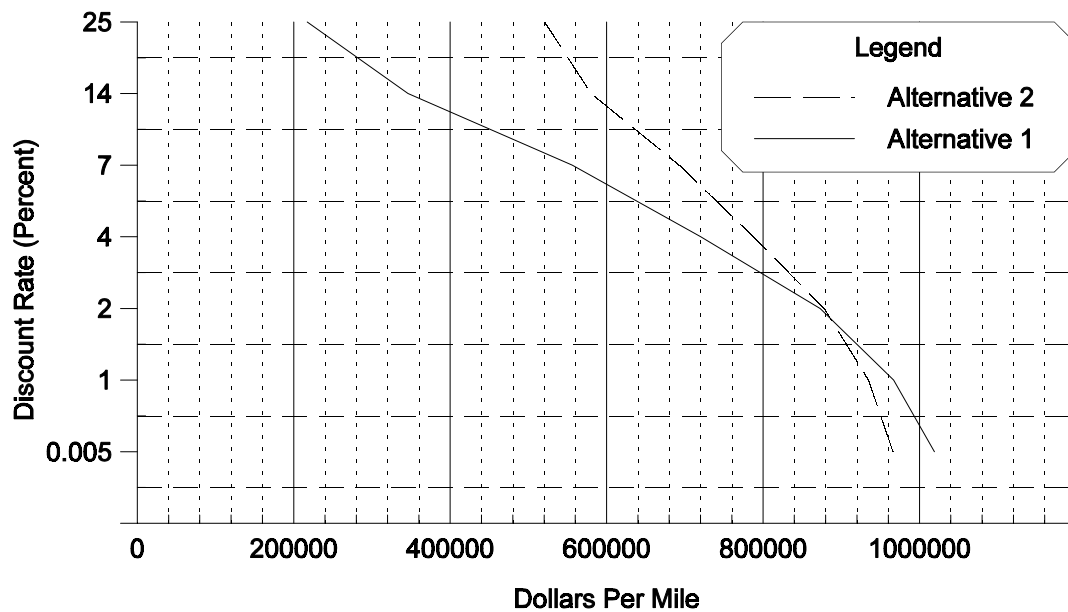
Discount Rate
 Analysis Period
 Maintenance Cost
 User Cost

<u>Present Worth Method</u> Example 2		
Discount Rate	Alternative 1	Alternative 2
0.5%	\$1,019,019	\$965,914
1%	\$966,867	\$934,423
2%	\$872,970	\$877,999
4%	\$720,204	\$787,392
7%	\$556,142	\$692,885
14%	\$346,246	\$580,171
25%	\$217,394	\$520,453

<u>Annual Worth Method</u> Example 2		
Discount Rate	Alternative 1	Alternative 2
0.5%	\$36,663	\$34,753
1%	\$37,464	\$36,207
2%	\$38,978	\$39,203
4%	\$41,650	\$45,535
7%	\$44,817	\$55,837
14%	\$49,445	\$82,850
25%	\$54,416	\$130,275

COMPARISON - PRESENT WORTH ALTERNATIVES

Example 2



COMPARISON - ANNUAL WORTH ALTERNATIVES

Example 2

